Numerical simulation and monitoring of the Cathedral of Syracuse in Sicily

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ABSTRACT: In the present paper the results from a recent monitoring campaign and numerical analysis performed on the ancient Cathedral of Syracuse in Sicily are presented. The Acoustic Emission (AE) technique is adopted to assess the damage pattern evolution. The localization of the propagating cracks is performed using six synchronized AE sensors. A clear correlation between the regional seismic activity and the AE acquisition data is shown. In fact the AE count rate presents peaks corresponding to the main seismic events. In addition, a numerical analysis of the Cathedral is presented. The nonlinear Finite Element model is particularly refined to account for the cracking in the most damaged pillar. Some recent seismic events in the area acted as crack propagators. The crack occurrence obtained from the numerical analysis agrees quite well with the crack localization provided by the AE monitoring.

1 INTRODUCTION

The Cathedral of Siracusa (Sicily – Italy) is located in the higher zone of the Ortigia island. This region of Sicily has been belonging to the UNESCO World Heritage List since 2005. The Cathedral of Syracuse is the result of the transformation of the ancient Athena’s Greek Temple (5th century B.C.), with modifications that have also been consequence of the damages caused by earthquakes. The ancient temple had fourteen lateral columns and six in the front. The Cathedral incorporated many of them, as it is nowadays still visible, while other columns of the present structure were built with the salvage remains from the temple cell. At the present time, the structure shows an extended damage pattern, especially in four of the nave pillars (Binda et al. 2007).

In recent years, the authors have been working on the development of a method for the assessment of materials and structures based on the spontaneous release of pressure waves originated by the evolution of damage. This monitoring technique, referred to as Acoustic Emission (AE), is non invasive and non destructive and therefore is ideally suited for the control of historic and monumental structures in seismic areas (Carpinteri & Lacidogna 2006a, 2006b, 2007). With this technique, if it is not known, the initial position of the damage can be determined with the aid of a multiplicity of sensors and through triangulation (Carpinteri et al. 2006a, 2006b, 2007a). Once the damaged portion of a structure has been located, it becomes possible to evaluate the stability of the evolving damage, which may either come gradually to a halt or propagate at an ever faster rate. In this study, the AE technique was used to determine the damage level in a pillar that was part of the vertical bearing structure of the Cathedral of Syracuse (Sicily).

Beside the experimental research, a numerical simulation based on the Finite Element Method is performed, which is able to catch the main non linear features of the mechanical behaviour such as fracture nucleation, fracture propagation and time dependency. The most damaged pillar has been modelled in details, providing an accurate description of the blocks interaction by means of discrete interface elements. The main goal is to link the dissipated energy, acquired from the acoustic emissions (AE), and the fracture localization with the results obtained numerically (Carpinteri et al. 2008). From the numerical model, it is possible to observe that cracks develop due to the seismic load, according to the experimental evidence from the AE acquisition.

2 SYRACUSE CATHEDRAL AND STATE OF PRESERVATION

In the 6th century AD, the 5th century B.C. Greek temple of Athena in Syracuse, was transformed into a Catholic Church, and successively became the Cathedral of the City; the building was frequently
modified along the centuries until the present configuration (Agnello 1950; Agnello 1996; Privitera 1863; Russo 1991, 1992).

Several styles and structural details belonging to the different times can be recognized: (i) in the external walls the ancient Greek columns and the filling wall between them of the Byzantine time, (ii) the baroque façade, (iii) the added apse and chapels. Furthermore, being Syracuse in a seismic area, the Cathedral was damaged, repaired or partially rebuilt several times (Agnello 1950; Agnello 1996). Figure 1 shows the evolution of the Cathedral plan along the centuries.

The Cathedral pillars have a peculiar interest; they had been obtained cutting out the stonework walls of the internal cell of the Greek temple. The pillars show several repaired areas, replacements, but also several cracks.

In order to evaluate their state of preservation, the extension and the depth of the replacements and the presence of internal defects, an investigation program was planned by the Sovrintendenza of Syracuse and the Politecnico of Milan. As a first step, a survey of the pillars with an accurate mapping of the superficial materials, of the defects, of the cracks and of the morphology was carried out. The crack pattern was classified and accurately documented and reported on the geometrical survey. Figure 2 gives an example of this documentation referred in a damaged pillar. The cracks display frequently a vertical pattern due to compressive stresses, whose action is often combined with the compressive-bending stresses caused by frequent earthquakes. In some cases, the corners and part of the stone blocks were expelled. The mortar traces in these cases are trials to locally repair the damages. In the survey repaired cracks were cleared in order to evaluate the evolution of the damages.

On the base of this detailed survey, NDT tests were performed in order to investigate the depth of the damage: (i) sonic and ultrasonic to find voids inside the pillars and the depth of the cracks respectively (in some cases up to 40 cm), (ii) thermovision to detect the detachment of renders and repaired parts, (iii) radar to find internal cracks and inclusions (Fig. 3).

The complementarity of these NDTs already studied in (Binda et al. 2000, Binda et al. 2003), could be successfully exploited to diagnose the state of damage of the pillars (Binda et al. 2006). Furthermore a monitoring of the cracks development carried out for approximately two years showed an evident trend to increase their size in some cracks of the pillars positioned at the end of the central nave, which suggested a further check of the damage by acoustic emission.

3 AE MONITORING

3.1 The monitored pillar

The AE monitoring process was performed on a pillar of the Cathedral of Syracuse. The temple had 14 columns along the sides and 6 at front, and some of them, belonging to the peristyle and the stylobate, can still be identified. In the layout of the Cathedral shown in Figure 4, all the pillars and the columns inside the building are marked with a progressive number.

Basically, the Doric columns are marked with numbers in three ranges: 1–8; 22, 23; 33–40; whereas the pillars, obtained from the calcareous stone masonry of
the temple cell, are identified with the remaining numbers. As said above, from the survey of the cracks, it was determined that the pillars in the most critical conditions were nos. 18, 19, 29 and 30, all of them located near the end of the central nave (Fig. 4). These pillars show an appreciable degree of deterioration, due to the presence of added layers of plaster and conspicuous cracks, which in some cases seem to cut the constituent stone blocks. Pillar no. 19, selected for the application of the AE monitoring technique, is shown in Figure 4 indicated by a circle.

The pillar no. 19 is one of the most damaged. This element together with pillar no 18, is situated toward the altar, and on this element a serious damage is observed. It is important to stress the effects of the 1542 earthquake, which produced a great deformation of the perimeter wall close to the pillars nos. 18 and 19. This could justify the bad state of preservation of these two pillars, characterized by the presence of detached covers and deep cracks on all the prospects. Despite the several intervention the section is reduced. The cracks in these pillars also show a large movement than elsewhere (Binda et al. 2007).

The pillar (save for a few strengthening works performed – according to the Syracuse Superintendence for Cultural Heritage – during a restoration process in 1926) was thought to be made of limestone blocks, probably installed during the initial construction of the temple dedicated to Athena in the 5th century B.C. The investigation revealed instead the presence of parts made with brick masonry ascribed to the interventions at the beginning of the 20th century (Fig. 5). The lower stiffness of these parts is probably the cause of the damage developed in the stones.

3.2 **AE equipment and “in situ” applications details**

Monitoring a structure by means of the AE technique proves possible to detect the occurrence and evolution of stress-induced cracks. Cracking, in fact, is accompanied by the emission of elastic waves which propagate within the bulk of the material. These waves can be received and recorded by piezoelectric (PZT) transducers applied to the surface of the structural elements. The signal is therefore analysed by a measuring system counting the emissions that exceed a certain voltage threshold measured in volts (V). The leading-edge equipment adopted by the authors for the analysis on the vertical bearing structures of the Syracuse Cathedral consists of six units USAM®, that can be synchronized for multi-channel data processing.

The most relevant parameters acquired from the signals (frequencies in a range between 50 and 800 kHz, arrival time, amplitude, duration, number of events and oscillations) are stored in the USAM memory and then downloaded to a PC for a multi-channel data processing (see Fig. 6). Microcracks localisation is performed from this elaboration and the condition of the monitored specimen can be determined (Carpinteri et al. 2006a, 2007a).

On each side of element 19 an evident cracking pattern is observed. The AE sensors have been applied on the middle part of the pillar as shown in Figure 7a and b. In the Figure 7a the zones with capillar vertical cracks are indicated by circles. The AE sensors arrangement is represented in Figure 7a according to the scheme
Figure 6. AE signal identified by the transducer.

Figure 7. View (a) and axonometric projection (b) of the AE sensor applied to the pillar 19.

Table 1. Arrangement of the sensors applied to the pillar 19.

<table>
<thead>
<tr>
<th>AE sensors</th>
<th>x [mm]</th>
<th>y [mm]</th>
<th>z [mm]</th>
</tr>
</thead>
<tbody>
<tr>
<td>S1</td>
<td>539.7</td>
<td>0.00</td>
<td>−285</td>
</tr>
<tr>
<td>S2</td>
<td>679.7</td>
<td>0.00</td>
<td>−455</td>
</tr>
<tr>
<td>S3</td>
<td>434.7</td>
<td>0.00</td>
<td>335</td>
</tr>
<tr>
<td>S4</td>
<td>394.7</td>
<td>0.00</td>
<td>265</td>
</tr>
<tr>
<td>S5</td>
<td>0.00</td>
<td>410</td>
<td>330</td>
</tr>
<tr>
<td>S6</td>
<td>0.00</td>
<td>300</td>
<td>−220</td>
</tr>
</tbody>
</table>

reported in Figure 7b. The positions of applied sensors are listed in Table 1, and the reference frame for the sensors position coordinates is shown in Figure 7b.

4 RESULT OF THE MONITORING PROCESS

The monitoring process began at 11:00 a.m. of 19 September 2006 and ended at 12:20 p.m. of 21 January 2007. The data collected were analysed in order to interpret the evolution of damage and determine the positions of AE sources within the pillar. The AE signal received by the transducers is processed by an analyser which counts the oscillations exceeding a certain voltage threshold. This makes it possible to plot cumulative curves reflecting the count number as measured continuously throughout the monitoring period. This method, referred to as Ring-Down Counting, is widely used for defect detection purposes (see Fig. 6). As a first approximation, in fact, the count number $N$, i.e., oscillations per unit time (differential function) can be compared with the quantity of energy released during the monitoring process, and the relative sums (cumulative function) may be assumed to increase proportionately with the widening of the damaged zone. Needless to say, this assumption applies only if the damage evolves slowly (Brindley et al. 1973; Pollock 1973; Swindlehurst 1973; Carpinteri & Lacidogna 2006a).

From the chart in Figure 8 it can be seen that the pillar is actually undergoing a deterioration process. If we examine the chart illustrating the differential function of AE counts, we can see sudden increases in the oscillation peaks occurring at certain intervals over time. It should be also noted that during the monitoring period, strong seismic actions were recorded in the area, within a radius of ca 50 km around the city of Syracuse. Earthquake data for the period were obtained from website: www.ct.ingv.it/Sismologia/GridSism.asp published by the Seismic Data Analysis Group of Catania (Gruppo di Analisi Dati Sismici – INGV-CT). From the wealth of data available, we selected the seismic events with a local magnitude (Ml) greater than 1.2 that had during the monitoring period. These events are illustrated in Figure 8, where the relative date and magnitude are also given.

The chart in Figure 8, showing AE monitoring and regional earthquake data, reveals an interesting correlation between the AE activities determined experimentally and seismic events: the timing of the energy peaks measured by means of the AE differential counts is seen to coincide almost invariably with seismic shocks. This correspondence seems to show how the pillar monitored behaves in a pseudo-stable manner when subject to the vertical loads alone, but has a meagre capacity to respond elastically to horizontal or oscillatory actions. A behaviour of this kind
was observed by the author during an earlier monitoring process carried out with the AE technique at site which was also subject to seismic activity (Carpinteri & Lacidogna 2006b, 2007). Thus, it may be stated that whilst the AE technique finds its primary application in non-destructive tests, it is also important to explore its potential as a monitoring tool in structures exposed to particular environmental conditions, such as seismic activities. As already pointed out by the authors, in fact, the two phenomena – acoustic emissions on a structural scale and seismic activities on a territorial scale – appear really similar and mutually correlative.

5 DETECTION OF DAMAGE IN THE MONITORED PILLAR

5.1 Localisation of AE sources
The first stage of the localisation method consists in recognising the data needed to identify the AE sources, followed by the triangulation procedure. During the first stage, the groups of signals, recorded by the various sensors, that fall into time intervals compatible with the formation of microcracks in the volume analysed, are identified. These time intervals, of the order of micro-seconds, are defined on the basis of the presumed speed of transmission of the waves ($P$) and the mutual distance of the sensors applied to the surface of the material. It is usual to assume that the amplitude threshold of 100 µV of the non-amplified signal is appropriate to distinguish between $P$-wave and $S$-wave arrival times. In fact, $P$-waves are usually characterized by higher value signals. In the second stage, when the formation of microcracks in a three-dimensional space is analysed, the triangulation technique can be applied if signals recorded by at least five sensors fall into the time intervals. Thus, with this procedure it is possible to define both the position of the microcracks in the volume and the speed of transmission of $P$-waves. The localisation procedure can also be performed through numerical techniques using optimisation methods such as the Least Squares Method (LSM) (Carpinteri et al. 2006a, 2007a).

In the present work, applying the localisation procedure more than 50 AE sources have been localised with a high confidence level. Considering previous applications of the AE technique carried out by the authors, the approximation for elements with large size is about ±10 mm (Carpinteri et al. 2006b). The localised sources and the cracking pattern for pillar no.19 are represented in Figure 9. It can be noted that the localised sources are concentrated near the more visible crack paths. The localisation of these source concentration (Fig. 9) and the oscillation counting (Fig. 8) denounce that the pillar is subject to a damaging phenomenon in slow but progressive evolution.

5.2 Time dependence of damage
The time dependence of the structural damage observed during the monitoring period, identified by parameter $\eta$, can also be correlated to the rate of propagation of the microcracks. If we express the ratio between the cumulative number of AE counts recorded during the monitoring process, $N$, and the number obtained at the end of the observation period, $N_d$, as a function of time, $t$, we get the damage time dependence on AE:

$$\eta = \frac{E_d}{N_d} = \left( \frac{t}{t_d} \right)^{\beta}.$$  

In equation (1), the values of $E_d$ and $N_d$ do not necessarily correspond to critical conditions ($E_d \leq E_{max}$; $N_d \leq N_{max}$) and the $t_d$ parameter must be construed as the time during which the structure has been monitored. By working out the $\beta$ exponent from the data obtained during the observation period, we can make a prediction as to the structure’s stability conditions. If $\beta < 1$, the damaging process slows down and the structure evolves towards stability conditions, in as much as energy dissipation tends to decrease; if $\beta > 1$ the process diverges and becomes unstable; if $\beta \approx 1$ the process is metastable, i.e., though it evolves linearly over time, it can reach indifferently either stability or instability conditions (Carpinteri & Lacidogna 2006b, 2007; Carpinteri et al. 2007b).

During the observation period, which lasted 121 days for the monitored pillar, the number of AE counts was $\approx 4300$ (Fig. 8). In order to obtain indications on the rate of the damage process, as given in Equation 1, the data obtained with the AE technique were subjected to best-fitting in the bilogarithmic plane. This yielded a slant $\beta = 0.98$ as shown in Figure 10. The result confirm that the damage process in the pillar is in metastable conditions according to a quasi-linear progression over time.
6 NUMERICAL SIMULATION

6.1 Laboratory tests and characteristic constants

Beside the experimental research, a numerical simulation based on the Finite Element Method is performed, which is able to catch the main non-linear features of the mechanical behaviour such as fracture nucleation, fracture propagation and time dependency. The main goal will be to link the dissipated energy, acquired from the acoustic emissions (AE), and the fracture localization with the results obtained numerically (Carpinteri et al. 2008). To this end a number of tests have been conducted in order to determine the mechanical properties of the Syracuse Cathedral stone.

The ancient stone used in the construction of the temple was located in the area of Plemmirio where archaeological studies have found the presence of various quarries of the Greek period. During the restoration works recently carried out the technique of replacing stone blocks was employed for several damaged elements. The removed elements were replaced by other blocks consisting of the same stone. In particular a portion of one of the removed elements has been used to define, through laboratory tests, the mechanical properties of the material that since 2400 years constitutes the bearing structure of the Cathedral (Fig. 11). Some cylindrical specimens having slenderness \( \lambda = 1 \), and diameter equal to 30, 60 and 120 mm respectively, were obtained from the stone block (Fig. 11a, b). Three specimens (a,b,c) for each diameter have been tested at the Fracture Mechanics Laboratory of Politecnico di Torino, in this way the ultimate peak stress \( (\sigma_u) \), and the elastic modulus \( (E) \) are computed (see Table. 2).

<table>
<thead>
<tr>
<th>Specimens</th>
<th>Peak load [kN]</th>
<th>Peak stress ( (\sigma_u) ) [Mpa]</th>
<th>Elastic mod. ( (E) ) [Mpa]</th>
</tr>
</thead>
<tbody>
<tr>
<td>1_a–c (Ø = 30)</td>
<td>7.12</td>
<td>10.7</td>
<td>1500</td>
</tr>
<tr>
<td>2_a–c (Ø = 60)</td>
<td>22.10</td>
<td>7.82</td>
<td>2015</td>
</tr>
<tr>
<td>3_a–c (Ø = 120)</td>
<td>96.59</td>
<td>8.54</td>
<td>2200</td>
</tr>
</tbody>
</table>

6.2 The numerical model

A detailed 3D model of the most damaged pillar has been obtained according to the geometrical survey. The geometry of each block, as well as the presence of masonry inserts have been considered. Fifteen-node isoparametric solid wedge elements have been used to discretize the more regular zones of the model, while ten-node, three-side isoparametric solid pyramid elements have been adopted for the more complicated ones. Interfaces between blocks have been modelled with triangular twelve-node quadratic interface elements.

The resulting model comprises 5081 elements and 9188 nodes. Figure 12 shows the mesh of the pillar, and the details of the masonry inserts acquired by the NDT analysis. The displacements at the base of the pillar were fixed, while the top of the pillar was elastically constraint, in order to account for the interaction with the surrounding structure of the Cathedral. Two main load were considered: the dead load (of the pillar and of the surrounding structure), and an horizontal seismic load provided as an horizontal ground acceleration.

Figure 13a shows a detail of the interface elements between each block of the pillar, while Figure 13b shows the deformed mesh under the effect of the dead load. The elastic modulus of the stone block, as deduced from the experimental test, was 2000 MPa, while the Poisson ratio was equal to 0.12. The mean compressive strength was equal to 9 MPa. For the present sandstone, an average tensile strength of 3 MPa, and fracture energy of 50 Nm were adopted.
It is worth noting that, under the effect of the sole gravity load, the maximum compressive stress do not exceed the value of 2 MPa, which is low compared with the strength of the sandstone. On the other hand, due to the heterogeneity of the pillar, tensile stresses may arise that approach the tensile strength.

A seismic load has also been considered. If a return period of 140 years takes place, an horizontal acceleration of 1.288 m/s² is applied (30% probability occurrence in a period of 50 years). In this case, the compressive and tensile stresses increases, as shown in Figure 14a. The pillar deforms mainly according to his first modal shape, as shown in Figure 14b.

Due to the horizontal acceleration, cracking can take place in the pillar. A detail of crack nucleation is shown in Figure 15. The crack occurrence provided by the analysis agrees quite well with the crack localization provided by the AE recording. Cracking
The evolution of damage in a pillar made of calcareous stone blocks that is part of the vertical bearing structure of the Syracuse Cathedral was evaluated using the AE technique. The data collected were analysed in order to interpret the evolution of damage and to determine the positions of AE sources within the pillar. From the charts plotted for the differential and cumulative functions of the AE signal counts it can be seen that the pillar is actually undergoing a damage process. Moreover, by applying the AE source localisation procedure it was possible to identify ca. 50 emission points within the pillar. Within the stone blocks to which the sensors had been applied, the points were seen to concentrate along the cracks that could be discerned more clearly on the surface. The identification of these emission sources together with the oscillation counts shows that the pillar is indubitably undergoing a slow but incessant damage process.

Beside the experimental research, using a numerical simulation based on the Finite Element Method, the most damaged pillar has been modelled in details, providing an accurate description of the blocks interaction by means of discrete interface elements. The numerical analysis has been performed considering the structure subjected to seismic horizontal loads. By this model the crack nucleation is found in the same positions identified through the AE monitoring. In this way the numerical model confirms the results obtained experimentally.

ACKNOWLEDGEMENTS

The financial support for AE application provided by the European Union (EU) Leonardo da Vinci Programme, ILTOF Project is gratefully acknowledged. Special thanks for their collaboration go to the Arch. M. Muti, to the Eng. R. Meloni and to the Arch. L. Regalbuto of the Soprintendenza of Syracuse. The Soprintendenza of Siracusa supported the all the other NDT research.

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